

A table of Fourier transforms and properties

Forward: $F(\nu) = \int_{-\infty}^{\infty} f(t) e^{-j2\pi\nu t} dt$

Inverse: $f(t) = \int_{-\infty}^{\infty} F(\nu) e^{j2\pi\nu t} d\nu$

Some properties

Some transform pairs

$$F(t) \longleftrightarrow f(-\nu)$$

$$\delta(t) \longleftrightarrow 1$$

$$f^*(t) \longleftrightarrow F^*(-\nu)$$

$$u(t) e^{-at} \longleftrightarrow \frac{1}{j2\pi\nu + a}$$

$$f(at) \longleftrightarrow \frac{1}{|a|} F\left(\frac{\nu}{a}\right)$$

$$u(t) \longleftrightarrow \frac{1}{2} \delta(\nu) + \frac{1}{j2\pi\nu}$$

$$f(t - t_0) \longleftrightarrow e^{-j2\pi\nu t_0} F(\nu)$$

$$\exp(j2\pi\nu_0 t) \longleftrightarrow \delta(\nu - \nu_0)$$

$$e^{j2\pi\nu_0 t} f(t) \longleftrightarrow F(\nu - \nu_0)$$

$$\cos(2\pi\nu_0 t) \longleftrightarrow \frac{1}{2} [\delta(\nu - \nu_0) + \delta(\nu + \nu_0)]$$

$$\frac{d^n}{dt^n} f(t) \longleftrightarrow (j2\pi\nu)^n F(\nu)$$

$$\sin(2\pi\nu_0 t) \longleftrightarrow \frac{1}{2j} [\delta(\nu - \nu_0) - \delta(\nu + \nu_0)]$$

$$-j2\pi t f(t) \longleftrightarrow \frac{dF(\nu)}{d\nu}$$

$$\Pi(t) \longleftrightarrow \text{sinc}(\nu)$$

$$\int_{-\infty}^t f(\tau) d\tau \longleftrightarrow \frac{1}{j2\pi\nu} F(\nu) + \frac{1}{2} F(0) \delta(\nu)$$

$$\text{sgn}(t) \longleftrightarrow \frac{1}{j\pi\nu}$$

$$(f * g)(t) \longleftrightarrow F(\nu) G(\nu)$$

$$\sum_{k=-\infty}^{\infty} \delta(t - kT) \longleftrightarrow \frac{1}{T} \sum_{k=-\infty}^{\infty} \delta\left(\nu - \frac{k}{T}\right)$$

$$f(t) g(t) \longleftrightarrow (F * G)(\nu)$$

$$\exp(-\pi t^2) \longleftrightarrow \exp(-\pi\nu^2)$$

$$\text{DFT: } X[r] = \frac{1}{N} \sum_{k=0}^{N-1} x[k] \exp\left(-\frac{j2\pi r k}{N}\right)$$

$$\text{IDFT: } x[k] = \sum_{r=0}^{N-1} X[r] \exp\left(\frac{j2\pi r k}{N}\right)$$

$$\text{Hilbert transform: } \hat{f}(t) = f(t) * \frac{1}{\pi t}$$

$$\text{Convolution integral: } (f * h)(t) = \int_{-\infty}^{\infty} f(\tau) h(t - \tau) d\tau$$